# Compiler Construction 

Lecture 5 - Top-Down Parsing

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## What is top-down parsing?

- Top-down parsing is a parsing-method where a sentence is parsed starting from the root of the parse tree (with the "Start" symbol), working recursively down to the leaves of the tree (with the terminals).
- In practice, top-down parsing algorithms are easier to understand than bottom-up algorithms.
- Not all grammars can be parsed top-down, but most context-free grammars can be parsed bottomup.


## An example of top-down parsing

Let's consider the expression grammar:
$\mathrm{E}::=\mathrm{E}+\mathrm{T} \mid \mathrm{T}$
$\mathrm{T}::=\mathrm{T} * \mathrm{~F} \mid \mathrm{F}$
F ::= id |const|(E)

How will it begin parsing the expression:

$$
3^{*} x+y^{*} z
$$

$$
\underset{\mathrm{E}+\mathrm{T}}{\mathrm{E}}
$$



F
const

## LL(k) grammars

- Top-down grammars are referred to as $\operatorname{LL}(\mathrm{k})$ grammars:
- The first L indicates Left-to-Right scanning.
- The second L indicates Left-most derivation
- The k indicates k lookahead characters.
- We will be examining LL(1) grammars, which spot errors at the earliest opportunity but provide strict requirements on our grammars.


## LL(1) grammars

- LL(1) grammars determine from a single lookahead token which alternative derivation to use in parsing a sentence.
- This requires that if a nonterminal A has two different productions:
A : : = $\alpha$
and
A ::= $\beta$
- that a and $\beta$ cannot begin with the same token.
$-\alpha \underline{\boldsymbol{o r}} \beta$ can derive an empty string but not both.
- if $\beta=>^{*} \varepsilon, \alpha$ cannot derive any string that begins with a token that could immediately follow A.


## LL(1) grammars (continued)

If you look at the first token of expression

$$
3^{*} x+y^{\star} z
$$

(which is const) and the productions for the start symbol E

$$
\mathrm{E}::=\mathrm{E}+\mathrm{T} \mid \mathrm{T}
$$

How can you tell whether it derives $\boldsymbol{E}+\boldsymbol{T}$ or simply $\boldsymbol{T}$ ? This requires information about the subsequent tokens.

## LL(1) grammars (continued)

It becomes necessary to convert many grammars into LL(1). The most common conversions involve:

- Removing left-recursion (whether it is direct or indirect)
- Factoring out any terminals found out the beginning of more than one production for a given nonterminal


## Removing left-recursion

- Aho, Sethi and Ullman show that left recursion of the form:

$$
\mathrm{A}::=\mathrm{A} \alpha \mid \beta
$$

can be converted to right-recursion (which $\underline{i s}$ LL(1)) by replacing it with the following productions:

$$
\begin{gathered}
\mathrm{A}::=\beta \mathrm{A}^{\prime} \\
\mathrm{A}^{\prime}::=\alpha \mathrm{A}^{\prime} \mid \varepsilon
\end{gathered}
$$

## Removing indirect left recursion

Indirect recursion has nonterminals appear on the right-hand side of productions which appear in its own right sentential form: e.g., $\quad \mathrm{A}::=\mathrm{B} \alpha \mid \mathrm{c}$

$$
\mathrm{B}::=\mathrm{B} \beta|\mathrm{~A} \delta| \mathrm{d}
$$

This can be removed by arranging the nonterminals in order and by then substituting for A in B 's right sentential form:

$$
\begin{aligned}
& \mathrm{A}::=\mathrm{B} \alpha \mid \mathrm{c} \\
& \mathrm{~B}::=\mathrm{B} \beta|\mathrm{~B} \alpha \delta| \mathrm{c} \delta \mid \mathrm{d}
\end{aligned}
$$

Now we simply eliminate the direct left-recursion:

$$
\begin{aligned}
& \mathrm{A}::=\mathrm{B} \alpha \mid \mathrm{c} \\
& \mathrm{~B}::=\mathrm{c} \delta \mathrm{~B}^{\prime} \mid \mathrm{d}^{\prime} \mathrm{B}^{\prime} \\
& \mathrm{B}^{\prime}::=\beta \mathrm{B}^{\prime}\left|\alpha \delta \mathrm{B}^{\prime}\right| \varepsilon
\end{aligned}
$$

## Left-Factoring

Many grammars have the same prefix symbols at the beginning of alternative right sentential forms for a nonterminal:
e.g., $A::=\alpha \beta \mid \alpha \gamma$

We replace these production with the following:

$$
\mathrm{A}::=\alpha \mathrm{A}^{\prime}
$$

$$
\mathrm{A}^{\prime}::=\beta \mid \gamma
$$

Converting an expression grammar into LL(1) form

- Our expression grammar is:

$$
\begin{gathered}
E::=E+T \mid T \\
T::=T^{*} F \mid F \\
F::=\mathbf{i d} \mid \text { const } \mid(E)
\end{gathered}
$$

- Following our rule for removing direct left-recursion, our grammar becomes:

$$
\begin{gathered}
E::=T E^{\prime} \\
E^{\prime}::=+T E^{\prime} \mid \varepsilon \\
T::=F T \\
T^{\prime}::=* F T^{\prime} \mid \varepsilon \\
F::=\mathbf{i d} \mid \text { const } \mid(E)
\end{gathered}
$$

## Parse Table

Once the grammar is in LL(1) form, we create a table showing which production we use in parsing each nonterminal for every possible lookahead token:

|  | E | E' | T | T' | F |
| :---: | :---: | :---: | :---: | :---: | :---: |
| + |  | 2 |  | 6 |  |
| * |  |  |  | 5 |  |
| ( | 1 |  | 4 |  | 9 |
| ) |  | 3 |  | 6 |  |
| id | 1 |  | 4 |  | 7 |
| const | 1 |  | 4 |  | 8 |
| \$ |  | 3 |  | 6 |  |

1 E ::= TE'
2 E' $::=+\mathrm{TE}$ '
$3 \quad \mathrm{E}^{\prime}::=\varepsilon$
$4 \quad \mathrm{~T}::=\mathrm{FT}$,
$5 \quad \mathrm{~T},:=$ *FT'
$6 \quad \mathrm{~T}^{\prime}::=\varepsilon$
$7 \quad \mathrm{~F}::=\mathrm{id}$
$8 \quad \mathrm{~F}::=$ const
$9 \quad \mathrm{~F}::=(\mathrm{E})$

## Parsing an expression using the LL(1) parse table

Let's take a look at the expression

$$
3 * x+y
$$

Our parse tree is initially just the start symbol $E$ and our lookahead token is const (the lexeme is $\mathbf{3}$ )

The production for E and a lookahead token of const is is \#1, making our parse tree

The production for T and a lookahead token of const is is \#4, making our parse tree:


## Parsing an expression using the LL(1) parse table (continued)

The production for F and a lookahead token of const is \#8, making our parse tree:
Since we have now matched the token, we get a new lookahead

The production for T' and a lookahead token of * is is \#5, making our parse tree:
We get another lookahead


## Parsing an expression using the LL(1) parse table (continued)

The production for F and a lookahead token of id is \#7, making our parse tree:
We get a new lookahead


The production for T' and a lookahead token of + is \#6, making our parse tree:

Parsing an expression using the LL(1) parse table (continued)

The production for E' and a lookahead token of + is \#2, making our parse tree:
We get a new
lookahead


The production for T and a lookahead token of id is \#4, making our parse tree:

## Parsing an expression using the LL(1) parse table (continued)

The production for F and a lookahead token of id is \#7, making our parse tree:
We get a new lookahead

Having reached the EOF

(represented by \$), the
productions for T' and E' are
6 and 3 respectively. Our
parse tree is complete.

## FIRST and FOLLOW sets

- Since LL(1) grammars are predictive (the first lookahead determines how we parse the nonterminal), the set of tokens that can appear at the beginning of any derivation for that nonterminal becomes extremely important. This is the FIRST set.
- Since LL(1) grammars include epsilon productions, the set of token that can appear immediately following the nonterminal becomes important in determining the FIRST set and is called the FOLLOW set.


## FIRST sets

- Definition: $\operatorname{FIRST}(\mathrm{A})$ (where A is a nonterminal) is the set of symbols beginning strings generated by A.
- Examples
$-\operatorname{FIRST}(E)=\{$ id, const, $( \}$
$\left.-\operatorname{FIRST}\left(E^{\prime}\right)=\{+),, \$\right\}$
$-\operatorname{FIRST}(T)=\{$ id, const, ( $\}$
$\left.-\operatorname{FIRST}\left(T^{\prime}\right)=\left\{+{ }^{*},\right), \boldsymbol{\$}\right\}$
$-\operatorname{FIRST}(\mathrm{F})=\{$ id, const, $( \}$


## FOLLOW sets

- Definition: FOLLOW(A) (where A is a nonterminal) is a set of symbol appearing to the right of A in a sentential form.
- Examples:
$-\operatorname{FOLLOW}(E)=\{ ), \$\}$
$\left.-\operatorname{FOLLOW}\left(\mathrm{E}^{\prime}\right)=\{ ), \$\right\}$
$-\operatorname{FOLLOW}(\mathrm{T})=(+),, \$\}$
$\left.-\operatorname{FOLLOW}\left(\mathrm{T}^{\prime}\right)=\{+),, \boldsymbol{\$}\right\}$
$-\operatorname{FOLLOW}(\mathrm{F})=\{*,+),, \$\}$


## Computing FIRST sets

To compute FIRST sets:
WHILE there are still terminals that may be added: FOR each production and for each nonterminal (in the form $\mathrm{A}::=\beta_{\mathrm{i}}$ :

IF $\beta_{1}$ is a terminal, add it to the FIRST set for
A (\& Production i)
ELSE IF $\beta_{1}$ is $\varepsilon$, add the FOLLOW set for A to the FIRST set for A (\& Production i)
$\operatorname{ELSE}\left(\beta_{1}\right.$ is a nonterminal), add the FIRST set
for $\beta_{1}$ to the FIRST set for A (\& Production i).

## Computing FOLLOW sets

Initialize FOLLOW(S) to $\{\$\}$
Initialize the other FOLLOW sets to $\}$
WHILE there are terminals that can be added:
FOR each nonterminal B:
Look for productions $\mathrm{P}_{\mathrm{i}}$ in the form $\mathrm{A}::=\alpha \mathrm{B} \gamma$
IF $\gamma$ is a terminal, add it to the set $\operatorname{FOLLOW}(\mathrm{B})$
ELSE IF $\gamma=\varepsilon$, add FOLLOW(A) to FOLLOW(B)
$\operatorname{ELSE}(\gamma$ is a nonterminal), add $\operatorname{FIRST}(\gamma)$ to FOLLOW(B)

Determining FIRST sets for LL(1) grammars
Let's take another look at our expression grammar in LL(1) form:
1 E ::= TE’ $\quad$ FIRST(1) $=$ FIRST(T)
$2 \mathrm{E}^{\prime}::=+\mathrm{TE} \quad \operatorname{FIRST}(2)=\{+\}$
$3 \mathrm{E}^{\prime}::=\varepsilon \quad \operatorname{FIRST}(3)=\operatorname{FOLLOW}\left(\mathrm{E}^{\prime}\right)$
4 T ::= FT, $\quad$ FIRST(4) $=\operatorname{FIRST}(\mathrm{F})$
5 T'::= *FT $\quad \operatorname{FIRST}(5)=\{*\}$
$6 \quad \mathrm{~T}^{\prime}::=\varepsilon \quad \operatorname{FIRST}(6)=\operatorname{FOLLOW}\left(\mathrm{T}^{\prime}\right)$
7 F ::= id $\quad \operatorname{FIRST}(7)=\{$ id $\}$
8 F ::= const $\quad$ FIRST $(8)=\{$ const $\}$
$9 \mathrm{~F}::=(\mathrm{E}) \quad \operatorname{FIRST}(9)=\{( \}$
It becomes useful to work with the $\operatorname{FIRST}(\mathrm{i})$, which is the first set for the derivations of the nonterminal coming from production i .

Determining FIRST sets for LL(1) grammars (continued)

FIRST(F) $=$ FIRST(7) U FIRST(8) U FIRST (9)

$$
=\{\text { id }, \text { const },( \}
$$

Therefore, $\operatorname{FIRST}(4)=\operatorname{FIRST}(\mathrm{F})=\{$ id, const, ( $\}$
Also, $\operatorname{FIRST}(\mathrm{T})=$ FIRST $(4)=\{$ id, const,$( \}$
1 E $::=\mathrm{TE} \quad \operatorname{FIRST}(1)=\{$ id, const, $( \}$
$2 \mathrm{E}^{\prime}::=+\mathrm{TE} \quad \operatorname{FIRST}(2)=\{+\}$
3 E' $::=\varepsilon \quad \operatorname{FIRST}(3)=\operatorname{FOLLOW}\left(\mathrm{E}^{\prime}\right)$
4 T $::=$ FT $\quad$ FIRST $(4)=\{$ id, const, ( $\}$
5 T' $::=* \mathrm{FT}, \quad \operatorname{FIRST}(5)=\{*\}$
$6 \quad \mathrm{~T}^{\prime}::=\varepsilon \quad \operatorname{FIRST}(6)=\operatorname{FOLLOW}\left(\mathrm{T}^{\prime}\right)$
7 F $::=\mathrm{id} \quad \operatorname{FIRST}(7)=\{$ id $\}$
$8 \quad \mathrm{~F}::=\mathrm{const} \quad$ FIRST $(8)=\{$ const $\}$
$9 \mathrm{~F}::=(\mathrm{E}) \quad \operatorname{FIRST}(9)=\{( \}$

Determining FIRST sets for LL(1) grammars (continued)
FOLLOW(E) is initially $\{\$\}$.
Since E is on the right side of Production \#9, we add) to the set.
Since E' is in both Productions 1 and 2 without anything following it (and Production is recursive, adding nothing), we add FOLLOW(E) to FOLLOW(E')
$\left.\operatorname{FOLLOW}\left(\mathrm{E}^{\prime}\right)=\operatorname{FOLLOW}(\mathrm{E})=\{ ), \$\right\}$

Similarly,
FOLLOW(T') $=\operatorname{FOLLOW}(T)=\operatorname{FIRST}\left(E^{\prime}\right)$ U FOLLOW(E')

$$
=\{+\} \cup\{ ), \$\}
$$

Determining FIRST sets for LL(1) grammars (continued) After determining the FOLLOW sets for E' and T', we have:

| 1 | $\mathrm{E}::=\mathrm{TE}$, | $\operatorname{FIRST}(1)=\{$ id, const, $( \}$ |
| :--- | :--- | :--- |
| 2 | $\mathrm{E}^{\prime}::=+\mathrm{TE}$, | $\operatorname{FIRST}(2)=\{+\}$ |
| 3 | $\mathrm{E}^{\prime}::=\varepsilon$ | $\operatorname{FIRST}(3)=\{ ), \boldsymbol{S}\}$ |
| 4 | $\mathrm{~T}::=\mathrm{FT}$, | $\operatorname{FIRST}(4)=\{$ id, const,$( \}$ |
| 5 | $\mathrm{~T}^{\prime}::=* \mathrm{FT}$, | $\operatorname{FIRST}(5)=\{*\}$ |
| 6 | $\mathrm{~T}^{\prime}::=\varepsilon$ | $\operatorname{FIRST}(6)=\{+),, \$\}$ |
| 7 | $\mathrm{~F}::=\mathrm{id}$ | $\operatorname{FIRST}(7)=\{$ id $\}$ |
| 8 | $\mathrm{~F}::=\mathrm{const}$ | $\operatorname{FIRST}(8)=\{$ const $\}$ |
| 9 | $\mathrm{~F}::=(\mathrm{E})$ | $\operatorname{FIRST}(9)=\{( \}$ |

How do we use this information in Parsing?
To determine which production to use in expanding a nonterminal.

## Parse Table - the final result

By looking up the token and nonterminal, we determine how to expand a given nonterminal.

We can build the parse recursively, or nonrecursively by using a stack.

|  | E | E' | T | T | F | 12 | $\begin{aligned} & \mathrm{E}::=\mathrm{TE} \\ & \mathrm{E}^{\prime}::=+\mathrm{TE} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| + |  | 2 |  | 6 |  |  |  |
| * |  |  |  | 5 |  | 3 | $\mathrm{E}^{\prime}::=\varepsilon$ |
| ( | 1 |  | 4 |  | 9 | 5 | $\begin{aligned} & \mathrm{T}::=\mathrm{FT} \mathrm{P}^{\prime} \\ & \mathrm{T}^{\prime}::=* \mathrm{FT}^{\prime} \end{aligned}$ |
| ) |  | 3 |  | 6 |  | 6 | T' $::=\varepsilon$ |
| id | 1 |  | 4 |  | 7 | 7 | F : $:=\mathrm{id}$ |
| const | 1 |  | 4 |  | 8 | 8 | $\mathrm{F}::=$ const |
| \$ |  | 3 |  | 6 |  |  | $\mathrm{F}::=$ (E) |

## The LL(1) JASON Grammar

1 Program ::= Header DeclSec Block .
2 Header ::= program identifier ;
3 DeclSec ::=VarDecls ProcDecls
4 VarDecls ::= VarDecl VarDecls
5 VarDecls $::=\varepsilon$
6 VarDecl ::= DataType IdList;
7 DataType ::= integer
8 DataType ::= real
9 IdList $::=$ identifier MoreIdList

## The LL(1) JASON Grammar (continued)

10 MoreIdList $::=$, identifier MoreIdList
11 MoreIdList $:=\varepsilon$
12 ProcDecls ::= ProcDecl ProcDecls
13 ProcDecls ::= $\varepsilon$
14 ProcDecl ::= ProcHeader DeclSec Block;
15 ProcHeader ::= procedure identifier ParamList ;
16 ParamList $::=($ ParamDecls $)$
17 ParamList ::= $\varepsilon$
18 ParamDecls ::= ParamDecl MoreParamDecls

## The LL(1) JASON Grammar (continued)

> 19 MoreParamDecls $::=$; ParamDecl MoreParamDecls
> 20 MoreParamDecls $::=\varepsilon$
> 21 ParamDecl $::=$ DataType identifier
> 22 Block $::=$ begin Statements end
> 23 Statements $::=$ Statement MoreStatements
> 24 MoreStatements $::=$; Statement MoreStatements
> 25 MoreStatements $::=\varepsilon$
> 26 Statement $::=$ read identifier
> 27 Statement $::=$ set identifier $=$ Expression

## The LL(1) JASON Grammar (continued)

## 28 Statement ::= write identifier

29 Statement $::=$ if Condition then Statements ElseClause endif

30 Statement $::=$ while Condition do Statements endwhile
31 Statement ::= until Condition do Statements enduntil
32 Statement $::=$ call identifier ArgList
33 Statement $::=\varepsilon$
34 ElseClause $::=$ else Statements
35 ElseClause $::=\varepsilon$
36 ArgList $::=($ Args $)$

## The LL(1) JASON Grammar (continued)

37 ArgList $::=\varepsilon$
38 Args ::= identifier MoreArgs
39 MoreArgs $::=$, identifier MoreArgs
40 MoreArgs $::=\varepsilon$
41 Condition $::=$ Expression RelOp Expression
42 RelOp $::==$
43 RelOp $::=$ !
44 RelOp $::=>$
45 RelOp $::=<$

## The LL(1) JASON Grammar (continued)

46 Expression $::=$ Term MoreExpression
47 MoreExpression $::=$ AddOp Term MoreExpression
48 MoreExpression $::=\varepsilon$
49 Term ::=Factor MoreTerm
50 MoreTerm $::=$ MultOp Factor MoreTerm
51 MoreTerm $::=\varepsilon$
52 Factor ::= identifier
53 Factor::= constant
54 AddOp ::=+

## The LL(1) JASON Grammar (continued)

55 AddOp $::=-$
56 MultOp $::=$ *
57 MultOp $::=$ /

## FIRST set for JASON

FIRST(1) $=$ FIRST ( Header $)=$ \{ program $\}$
FIRST(2) $=\{$ program $\}$
FIRST(3) $=$ FIRST $($ VarDecls $)=$ FIRST $($ VarDecl $)$
$\operatorname{FIRST}(4)==\operatorname{FIRST}($ VarDecl $)=\operatorname{FIRST}($ DataType $)$
FIRST(5) $=$ FOLLOW $($ VarDecls $)=$ FIRST(ProcDecls)
= FIRST(ProcDecl) U FOLLOW ( ProcDecls )
$\operatorname{FIRST}(6)=\operatorname{FIRST}($ DataType $)=\{$ real, integer $\}$
$\operatorname{FIRST}(7)=\{$ real $\}$
FIRST(8) $=\{$ integer $\}$
FIRST(9) $=\{$ identifier $\}$

FIRST set for JASON (continued)
$\operatorname{FIRST}(10)=\{$,
FIRST(11) $=$ FOLLOW $($ MoreIdList $)=$ FOLLOW $($ IdList $)$
= FOLLOW(VarDecl)

FIRST(12) $=$ FIRST $($ ProcDecl $)=$ FIRST $($ ProcHeader $)=\{$ procedure \}
FIRST(13) $=$ FOLLOW $($ ProcDecls $)=$ FIRST $($ Block $)=\{$ begin $\}$
FIRST(14) $=$ FIRST $($ ProcHeader $)=\{$ procedure $\}$
FIRST(15) $=$ \{ procedure $\}$
FIRST(16) $=\{( \}$
FIRST(17) $=$ FOLLOW $($ ParamList $)=\{;\}$

FIRST set for JASON (continued)
FIRST(18) $=$ FIRST $($ ParamDecl $)=$ FIRST(ParamDecl)
$=\operatorname{FIRST}($ DataType $)=\{$ integer, real $\}$
$\operatorname{FIRST}(19)=\{;\}$
FIRST(20) $=$ FOLLOW $($ MoreParamDecls $)=$ FOLLOW $($ ParamDecls $)=\{$ ) $\}$
FIRST(21) $=\operatorname{FIRST}($ DataType $)=\{$ integer, real $\}$
FIRST(22) $=\{$ begin $\}$
FIRST(23) $=$ FIRST(Statement)
FIRST(24) $=\{;\}$
FIRST(25) $=$ FOLLOW $($ MoreStatements $)=$ FOLLOW(Statement)

FIRST set for JASON (continued)
$\operatorname{FIRST}(26)=\{$ read $\}$
FIRST(27) $=\{$ set $\}$
FIRST(28) $=\{$ write $\}$
FIRST(29) $=\{$ if $\}$
FIRST(30) $=\{$ while $\}$
FIRST(31) $=\{$ until $\}$
$\operatorname{FIRST}(32)=\{$ call $\}$
FIRST(33) $=$ FOLLOW (Statement $)$
FIRST(34) $=\{$ else $\}$
FIRST(35) $=$ FOLLOW $($ ElseClause $)=\{$ endif $\}$
$\operatorname{FIRST}(36)=\{( \}$

FIRST set for JASON (continued)
FIRST $(37)=$ FOLLOW $($ ArgList $)=$ FOLLOW $($ Statement $)$
$\operatorname{FIRST}(38)=\{$ identifier $\}$
$\operatorname{FIRST}(39)=\{$,
$\operatorname{FIRST}(40)=\operatorname{FOLLOW}($ MoreArgs $)=\{ )\}$
FIRST(41) $=\operatorname{FIRST}($ Expression $)$
$\operatorname{FIRST}(42)=\{=\}$
$\operatorname{FIRST}(43)=\{!\}$
$\operatorname{FIRST}(44)=\{>\}$
$\operatorname{FIRST}(45)=\{<\}$
$\operatorname{FIRST}(46)=\operatorname{FIRST}($ Term $)=\operatorname{FIRST}($ Factor $)$
$\operatorname{FIRST}(47)=\operatorname{FIRST}(A d d O p)=\{+,-\}$

FIRST set for JASON (continued)
$\operatorname{FIRST}(48)=$ FOLLOW $($ MoreExpression $)$
$\operatorname{FIRST}(49)=\operatorname{FIRST}($ Factor $)$
$\operatorname{FIRST}(50)=\operatorname{FIRST}(\mathrm{MultOp})=(*, /\}$
FIRST(51) $=$ FOLLOW (MoreTerm $)$
$\operatorname{FIRST}(52)=\{$ identifier $)$
FIRST(53) $=\{$ constant $\}$
$\operatorname{FIRST}(54)=\{+\}$
$\operatorname{FIRST}(55)=\{-\}$
$\operatorname{FIRST}(56)=\{*\}$
$\operatorname{FIRST}(57)=\{/\}$

Determining the FIRST set for JASON
Let's determine the FIRST sets for the nonterminals:
FIRST(3) $=$ FIRST(4) $=$ FIRST ( (arDecl $)=$ FIRST(DataType) $=\{$ integer, real $\}$
FIRST(23) $=$ FIRST(Statement) $=$ FIRST(26) $\cup$ FIRST(27) $\cup$ FIRST $(28) \cup$ FIRST $(29) \cup$ FIRST $(30) \cup \operatorname{FIRST}(31) \cup$ $\operatorname{FIRST}(32) \cup \operatorname{FIRST}(33)=\{$ read, set, write, if, while, until, call $\} \cup$ FOLLOW(Statement)
FIRST(41) $=\operatorname{FIRST}(46)=\operatorname{FIRST}(49)=\operatorname{FIRST}($ Expression $)$
$=\operatorname{FIRST}($ Term $)=\operatorname{FIRST}($ Factor $)=\{$ identifier, constant \}

## Determining the FIRST set for JASON (continued)

Now we must find the necessary FOLLOW sets:
FIRST( 5) $=$ FIRST(ProcDecl) U FOLLOW ( ProcDecls $)=\{$ procedure \} U FOLLOW $($ DeclSec $)=\{$ procedure, begin $\}$
$\operatorname{FIRST}(11)=$ FOLLOW $($ IdList $)=$ FOLLOW $($ VarDecl $)=\{$ integer, real, procedure, begin \}
$\operatorname{FIRST}(25)=\operatorname{FOLLOW}(33)=\operatorname{FOLLOW}(37)=\operatorname{FOLLOW}($ Statement $)=$ FOLLOW(MoreStatements) $=\{;$, end, endif, endwhile, enduntil, else \}
FIRST(48) $=$ FOLLOW ( MoreExpression $)=$ FOLLOW ( Condition $)$
$=\{$;, end, endif, endwhile, enduntil, else, then, do \}
$\operatorname{FIRST}(51)=\operatorname{FIRST}($ MoreExpression $) \mathrm{U}$ FOLLOW( Expression $)=$ $\{+$, ;, end, endif, endwhile, enduntil, else, then, do \}

## Implementing the Parse Table

// The production table for predictive parsing.
// The nonzero entries are the production numbers for a // particular nonterminal matched with a lookahead token // Zero entries means that there is no such production // and it is a parsing error.
const int prodtable[][numtokens+3] $=\{$
/*Program*/ $\{0,0,0,0,0,0,0,0,0,0,0,0,0$, $1,0,0,0,0,0,0,0,0,0,0,0,0$, $0,0,0,0,0,0,0,0,0,0,0\}$,
/*Header*/ $\{0,0,0,0,0,0,0,0,0,0,0,0,0$, $2,0,0,0,0,0,0,0,0,0,0,0,0$, $0,0,0,0,0,0,0,0,0,0,0\}$,
/*DeclSect*/ \{ 3, $0,0,0,0,0,0,0,0,0,3,0,3$, $0,0,3,0,0,0,0,0,0,0,0,0,0$, $0,0,0,0,0,0,0,0,0,0,0\}$,

Implementing the parse table (continued)

```
/*VarDecls*/ { 5, 0, 0, 0, 0, 0, 0, 0, 0, 0, 4, 0, 5,
    0, 0, 4, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0},
/*VarDecl*/ { 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 6, 0, 0,
    0, 0, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0},
/*DataType*/ { 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 7, 0, 0,
    0, 0, 8, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0},
/*IdList*/ { 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    0, 0, 0, 0, 0, 0, 0, 0, 0, 9, 0},
/*MoreIdList*/{ 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    0,11,10, 0, 0, 0, 0, 0, 0, 0, 0, 0},
```


## The Parsing Algorithm

Processing context-free expressions requires the use of a stack. The Parsing algorithm uses a stack:

Place the start symbol in a node and push it onto the stack.
Fetch a token
REPEAT
Pop a node from the stack
IF it contains a terminal, match it to the current token (no match indicates a parsing error) and fetch another token
ELSE IF it contains a nonterminal, look it up in the production table using the nontermina and the current token. Place the variables in REVERSE order on the stack
UNTIL the stack is empty

## Recursive-Descent Parsing

- Recursive-descent parsing is a top-down parsing technique which shows a series of recursive procedures to parse the program
- There is a separate procedure for each individual nonterminal.
- Each procedure is essentially a large if-then-else structure which looks for the appropriate tokens when the grammar requires a particular terminal and calls another procedure recursively when the grammar requires a nonterminal.

Recursive descent parsing of JASON

```
class parser : scanner {
```

public:
parser (int argcount, char *args[]);
parser (void) ;
void ProcProgram(void) ;
private:
void ProcHeader (void) ;
void ProcDeclSec (void) ;
... ...
void error(char message[], int linenum);
tokentype thistoken;
int tabindex, level;
\};

```
symboltable
                                    st;
// main() - Just a simple-minded driver
int main(int argc, char *argv[])
{
        parser p(argc, argv);
        p.ProcProgram();
        st.dump();
        return(0);
}
parser::parser(int argcount, char *args[])
                : scanner (argcount,args)
{
        level = 0;
        thistoken = gettoken(tabindex);
}
```

```
void parser::ProcProgram(void)
{
    level++;
    cout << level << '\t' << "Program" << endl;
    // Program ::= Header DeclSec Block .
    ProcHeader();
    ProcDeclSec();
    ProcBlock() ;
    if (thistoken != tokperiod)
        error("Expected \".\"", linenum);
    getchar();
    ++level;
}
```

```
void parser::ProcHeader(void)
{
    level++;
    cout << level << '\t' << "Header" << endl;
    // Header ::= program identifier ;
    if (thistoken != tokprogram)
        error("Expected \"PROGRAM\"", linenum);
    cout << level+1 << '\t' << "program" << endl;
    thistoken = gettoken(tabindex);
    if (thistoken != tokidentifier)
        error("Expected identifier", linenum);
    cout << level+1 << '\t' << "identifier"
        << endl;
    thistoken = gettoken(tabindex);
```

```
    if (thistoken != toksemicolon)
            error("Expected \";\"", linenum);
    cout << level+1 << '\t' << ";" << endl;
    thistoken = gettoken(tabindex);
    --level;
}
void parser::ProcDeclSec(void)
{
    level++;
    cout << level << '\t' << "DeclSec" << endl;
    // DeclSec ::= VarDecls ProcDecls
    ProcVarDecls();
    ProcProcDecls();
    --level;
}
```

