

Coherent Control of Four-Wave Mixing Gain

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Outline

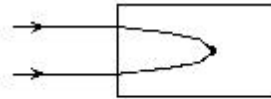


- **Filamentation Basics**
- **Filamentation Reduction--Theory and Experiment**
- **Two-Beam Experiment: Self-Diffraction**
- **Two-Beam Experiment: Conical Emission**
- **Future Work and Conclusions**

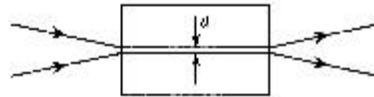
Filamentation Basics

For a material with a real, positive nonlinearity, there is a given power (P_{cr}) above which propagation leads to significant changes in the beam.

Self-Focusing, $P > P_{cr}$



Self-Trapping, $P = P_{cr}$

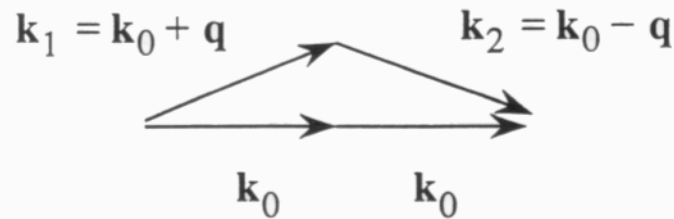


Filamentation, $P \gg P_{cr}$



Filamentation Basics

Filaments Grow From Perturbations (classical or quantum) on the Wavefront Via a Near-Forward Four-Wave Mixing Process:



Energy is Depleted From the Main Beam and Added to the Side Modes, With Gain Dependent on q :

$$A_1(z) = (A_1^+ e^{g+z} + A_1^- e^{g-z}) e^{i\Delta kz/2}$$

$$g = q (n_2 E^2 / n - q^2 / 4k^2)^{0.5}$$

Filamentation Reduction Theory

Let A_1 and A_2 be the side-mode amplitudes:

$$A_1(z) = \frac{1}{2} \left[A_1(0) + \frac{\kappa}{g} A_2^*(0) \right] e^{gz} + \frac{1}{2} \left[A_1(0) - \frac{\kappa}{g} A_2^*(0) \right] e^{-gz}$$

$$A_2^*(z) = \frac{1}{2} \left[A_2^*(0) + \frac{g}{\kappa} A_1(0) \right] e^{gz} + \frac{1}{2} \left[A_2^*(0) - \frac{g}{\kappa} A_1(0) \right] e^{-gz}$$

where: $\kappa = \frac{6\pi i \omega}{nc} \chi^{(3)} A_0^2$ and $\kappa/g = i$.

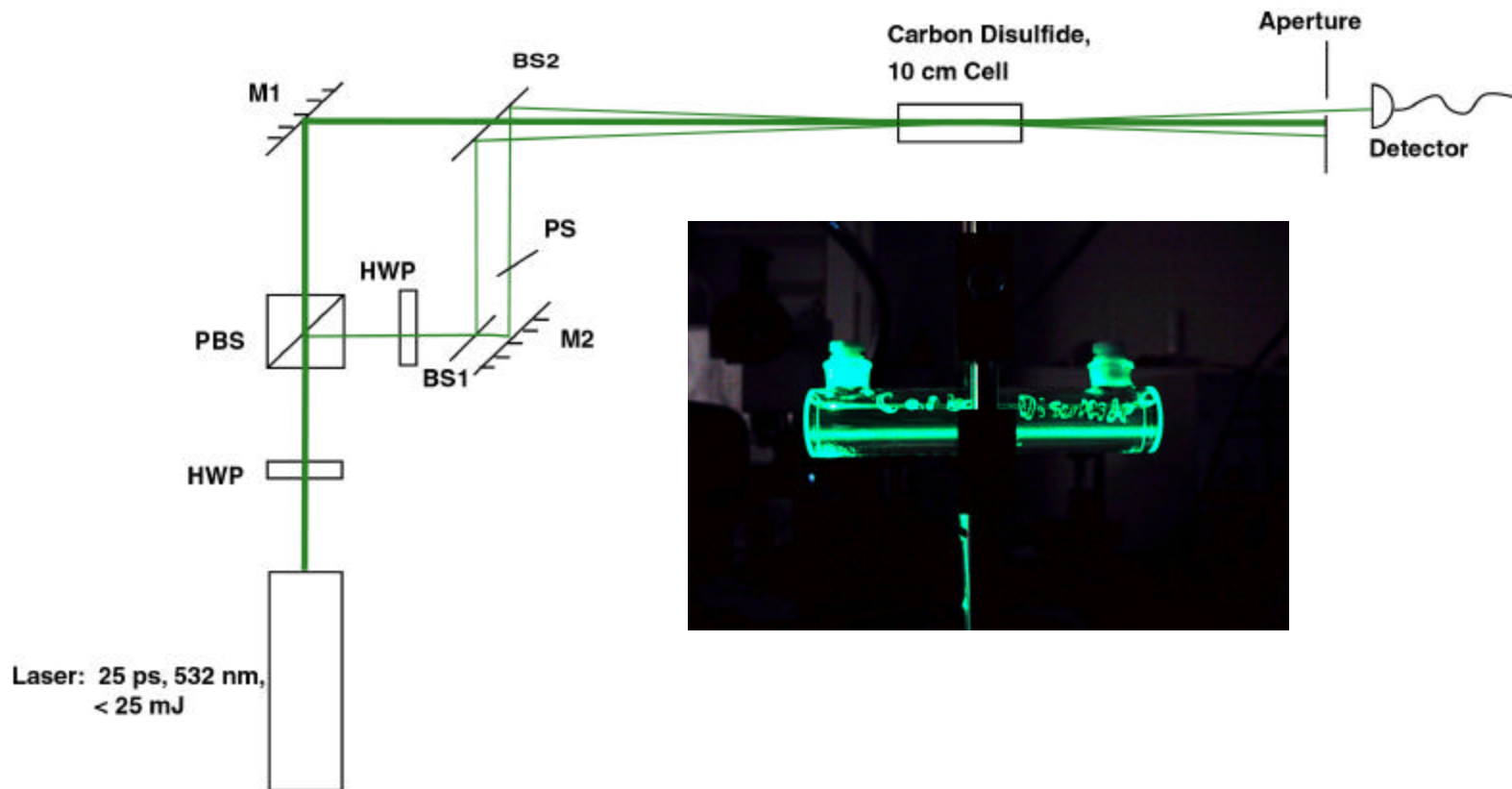
If set the relative side-mode phases such that: $\frac{A_2^*(0)}{A_1(0)} = i$

then side-modes will experience **no gain**.

R. W. Boyd and G. S. Agarwal, Phys. Rev. A 59, 2587 (1999).

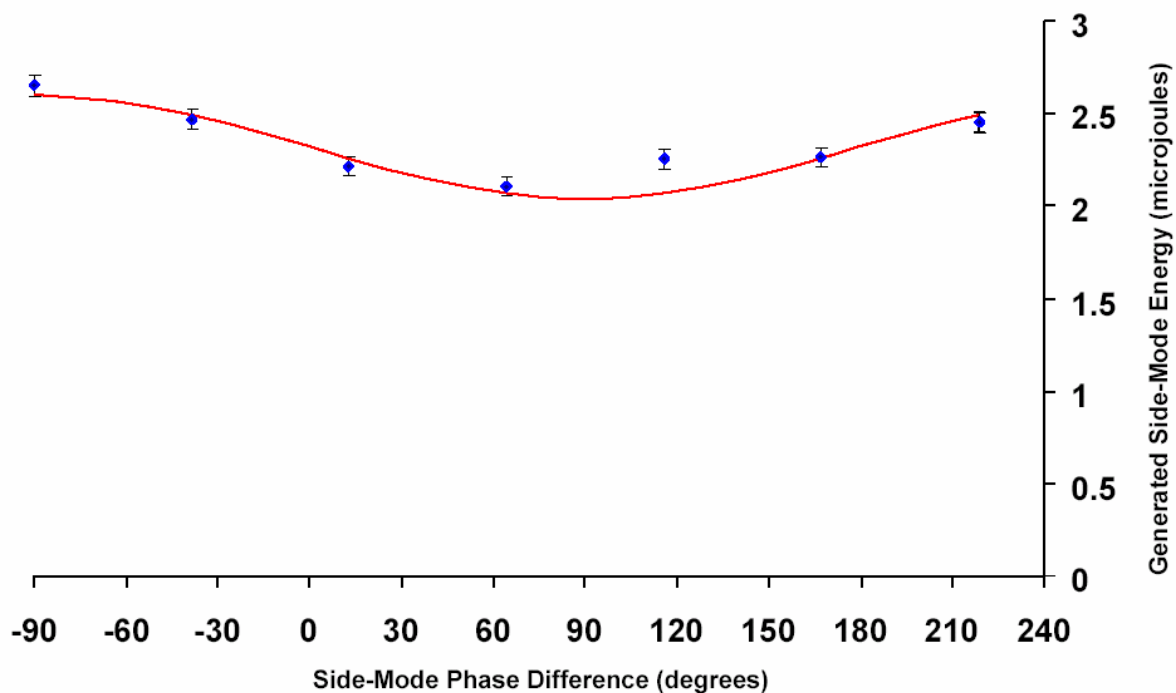


Filamentation Reduction Experiment



Filamentation Reduction Data

Experimental Data



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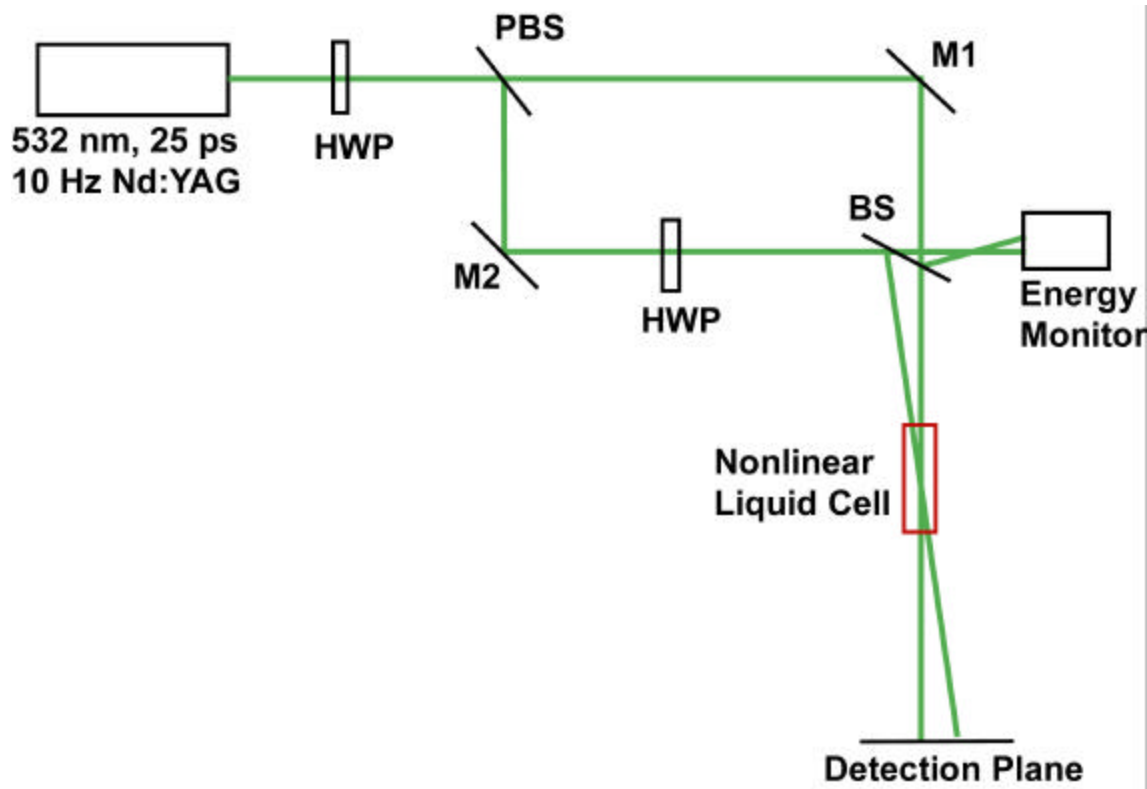
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Two-Beam Experiments

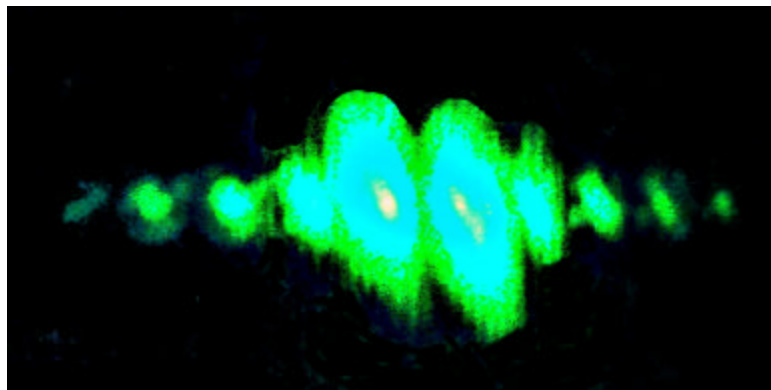
- **Use of two intersecting beams to reduce filamentation**
 - **Maillotte et al., Opt. Comm. 109, 265 (1994)**
- **Experimental & theoretical studies of pattern generation from two intersecting beams:**
 - **Kauranen et al., JOSA B 10, 2298 (1993)**
Theoretical treatment
 - **Chalupczak et al., Opt. Comm. 111, 613 (1994)**
Experimental treatment in barium vapor

Two-Beam Coupling Experiments



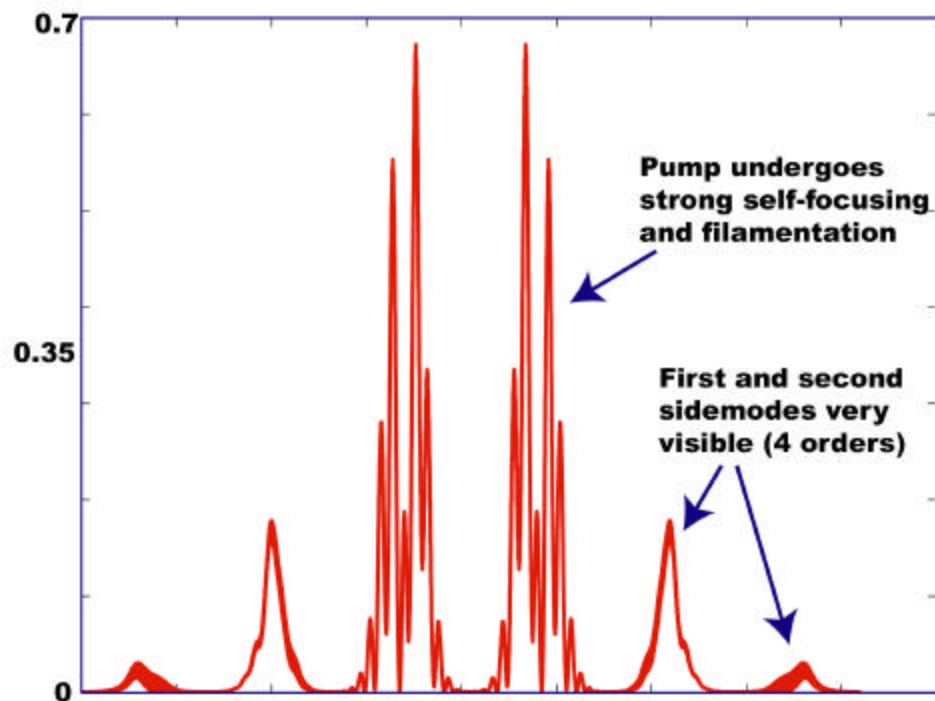
- Used 3-cm and 10-cm cells
- Used CS_2 , CCl_4 , and toluene
- Pulse intensities $\sim 1\text{-}80 \text{ MW/cm}^2$
- Crossing angles $\sim 0.003\text{-}0.04 \text{ rad}$

Two-Beam Coupling: Self-Diffraction

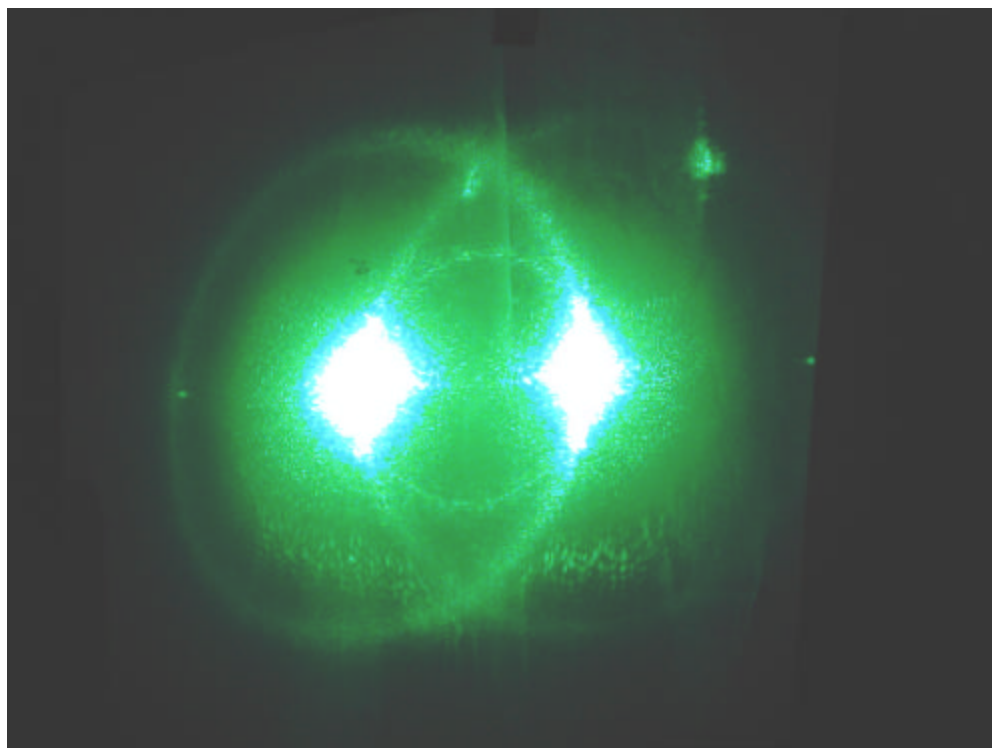


- Transverse intensity profile output:

10-cm CS₂ cell
 $q = 3.2 \times 10^{-3}$ rad
 $I = 11.3$ MW/cm² (each)
 $w_0 = 2.32$ mm

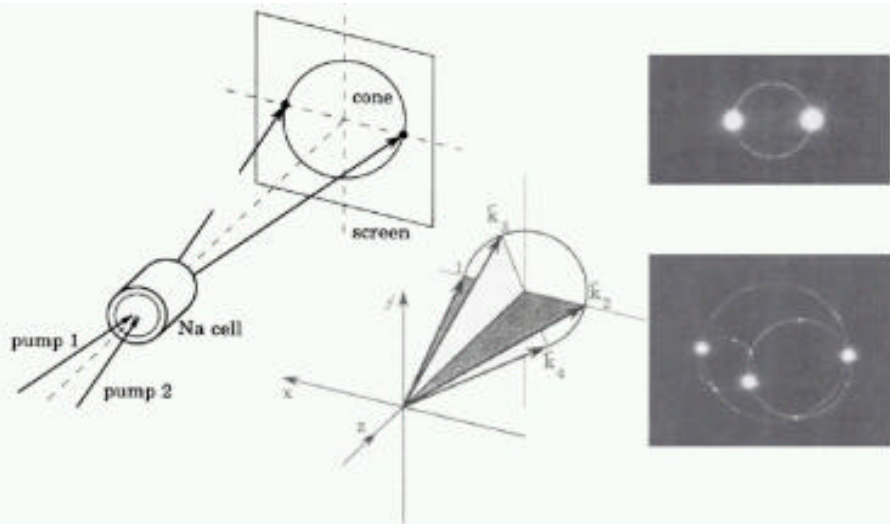


Two-Beam Coupling: Conical Emission

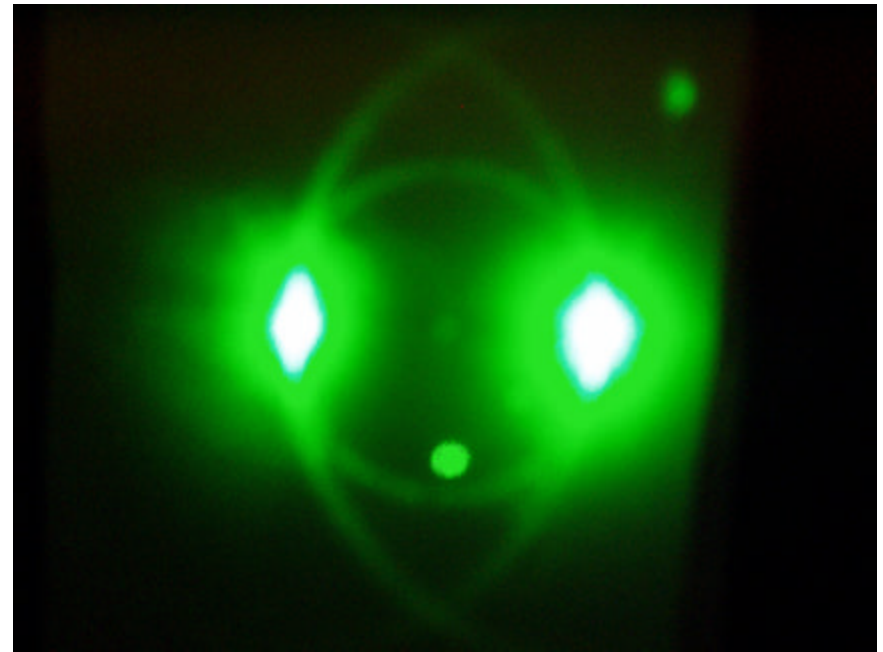


- At “large” angles (~ 0.03 rad), cones of light are observed
- Two types: cones centered about one beam and pass through the other, and cones connecting two beams (TBECE)
- Properties of the cones are primarily dependent upon beam which they intersect
- Clearly observable thresholds

Two-Beam Coupling: Conical Emission



Kauranen et al, Opt. Lett. 16, 943, 1991; Kauranen and Boyd, Phys. Rev. A, 47, 4297, 1993.



Possible Future Work



- **Optimize filamentation reduction experiment**
- **Explore other methods of filamentation reduction**
- **Investigate quantum-induced filamentation**
- **Search for correlations in two-beam generated patterns**

Conclusions



- **Demonstrated a method for filamentation reduction**
- **Studied related two-beam interactions in nonlinear liquids**
- **Witnessed self-diffraction, two-beam excited conical emission, and seeded spatial modulation instability**

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